Print and complete all work ON THIS PAPER. Submit your completed Lab 0 at the first lab session.

**Part I: Calculus II Readiness Quiz**

Work the problems below *without a calculator, reference materials or help*. Show all supporting steps and answer in exact values, not decimal approximations. Answers without accurate supporting work are not accepted. Simplify your final answers.

1. (2 pts.) Find the derivative of \( f(x) = \sqrt{\sin x \cos x} \). Final answer should be a fractional expression containing a radical.

2. (2 pts.) Let \( x = 10 \sin \theta \). Label all three sides of the right triangle with the appropriate constant or expression in \( x \).
3. (1 pt.) Give the exact value of each. (Remember, no calculator. No supporting work is needed.)

(a) \( \cos \left( \frac{7\pi}{6} \right) \)  
(b) \( \sin \left( \frac{3\pi}{4} \right) \)

4. (3 pts.) (a) Sketch the curves \( y = x \) and \( y^2 = x + 2 \) on the coordinate plane provided. (b) Calculate the coordinate pair(s) where the curves \( y = x \) and \( y^2 = x + 2 \) intersect.

(Remember, no calculator.)

5. (2 pts.) Calculate each limit.

(a) \( \lim_{x \to \infty} \frac{5x^2 - 17}{2x^2 + 3 - x} \)
(b) \( \lim_{b \to \infty} \tan^{-1} \left( \frac{b}{2} \right) \)
Part II: Review of sections 5.1-5.4

Here, you will review some of the concepts of integration that you learned at the end of Math 111 or similar course. Work the problems in the spaces below, reviewing the material in the book as much as necessary. No other assistance is allowed. A calculator may be used for calculations on problem 1 (a).

1. (2 pts.) (Section 5.1) (a) Approximate the area under \( f(x) = 2 + x^2 \) on the interval \([0, 3]\) using \( R_6 \).
    (b) Illustrate this approximation.

2. (2 pts.) (Section 5.2) The graph of \( g \) consists of two straight lines and a semicircle. Use it to evaluate each integral.

\[
\begin{align*}
(a) & \int_{2}^{6} g(x) \, dx \\
(b) & \int_{0}^{7} g(x) \, dx
\end{align*}
\]
3. (1 pt. each) (Sections 5.3 and 5.4) Evaluate each or explain why it cannot be evaluated using methods taught in these sections.

(a) \[ \int_{-1}^{3} \left( \frac{1}{x} \right) \, dx \]

(b) \[ \int (1-t)(t-4) \, dt \]

(c) \[ \int_{1}^{4} \frac{1+\sqrt{x}}{x} \, dx \]

4. (3 pts.) (Section 5.3) Let \( g(x) = \int_{0}^{x} f(t) \, dt \), where \( f \) is a continuous function on \([0, 4]\) as shown below.

(a) Evaluate \( g(0) \).

(b) Evaluate \( g(4) \).

(c) On what interval is \( g \) increasing?

(d) Where does \( g \) have a global maximum value?

(e) Sketch the graph of \( g(x) \) on the same coordinate plane.